

Non-Linear Analysis of Axially Loaded Built-Up Open Section Cold-Formed Columns

mai mohamed sheta

Department of construction and building Engineering, Higher Institute for Engineering, 6th of October City, Egypt, maisheta39@gmail.com

Hanan Hussein Eltobgy

Department of Civil Engineering, Faculty of Engineering at Shoubra, Benha University, Egypt, hanan.altobgy@feng.bu.edu.eg

Mohamed Massoud El Saadawy

Housing and Building National Research Center (HBRC), 87 El Tahrir St., Dokki, Giza 11511, PO Box 1770, Cairo, Egypt, m_massoud2002@yahoo.com

Khaled abdallah Gharib

Department of Civil Engineering, Faculty of Engineering at Shoubra, Benha University, Egypt, khaled.Gharib@feng.bu.edu.eg

Follow this and additional works at: <https://digitalcommons.aaru.edu.jo/erjeng>



Part of the [Structural Engineering Commons](https://digitalcommons.aaru.edu.jo/erjeng)

Recommended Citation

sheta, mai mohamed; Eltobgy, Hanan Hussein; El Saadawy, Mohamed Massoud; and Gharib, Khaled abdallah () "Non-Linear Analysis of Axially Loaded Built-Up Open Section Cold-Formed Columns," *Journal of Engineering Research*: Vol. 9: Iss. 1, Article 18.

DOI: <https://doi.org/10.70259/engJER.2025.911908>

Available at: <https://digitalcommons.aaru.edu.jo/erjeng/vol9/iss1/18>

This Article is brought to you for free and open access by Arab Journals Platform. It has been accepted for inclusion in Journal of Engineering Research by an authorized editor. The journal is hosted on [Digital Commons](https://digitalcommons.aaru.edu.jo/), an Elsevier platform. For more information, please contact marah@aarj.edu.jo, rakan@aarj.edu.jo.

Non-Linear Analysis of Axially Loaded Built-Up Open Section Cold-Formed Columns

Mai M.Sheta^{1*}, Hanan H. Eltobgy², Mohamed M. El-Saadawy³, and Khaled A. M. Gharib⁴

¹ Department of construction and building Engineering, Higher Institute for Engineering, 6th of October City, Egypt

²Department of Civil Engineering, Faculty of Engineering at Shoubra, Benha University, Egypt

³Housing and Building National Research Center (HBRC),87El Tahrir St., Dokki, Giza11511, POBox1770, Cairo, Egypt

⁴Department of Civil Engineering, Faculty of Engineering at Shoubra, Benha University, Egypt

*Corresponding author's email: maisheta39@gmail.com

Abstract- Built-up open cold-formed sections are commonly used in entrances, structural corners, and window frames. These elements exhibit low torsional stiffness and are highly susceptible to cross-sectional deformation. Battered built-up cold-formed steel (CFS) open columns offer enhanced load-carrying capacity when individual profiles cannot withstand applied loads. Extensive research has focused on understanding the buckling behavior of these structural elements. However, limited studies have explored the impact of spacing between cold-formed C-channel sections. Existing research suggests that battered columns with adequately spaced members exhibit superior structural performance compared to those with closely spaced channels. A critical factor affecting the performance of battered columns is the slenderness ratio of the unsupported length (L_z) between batten plates. Despite its significance, this aspect has been insufficiently explored in prior studies. The literature lacks defined limiting values for different column slenderness ratios, back-to-back distances between channel sections, and unsupported lengths between batten plates. Consequently, design methods proposed by various researchers may be unreliable. This study investigates the performance of axially loaded pin-ended columns, comprising two appropriately spaced lipped C-channels arranged back-to-back to form open built-up sections. Finite element models were developed using the ABAQUS platform and validated against test results from the literature. Following validation, the models were used for a comprehensive parametric analysis by varying key parameters, such as back-to-back distance, depth-to-width ratios, number of battens, column slenderness

ratios, and the relative slenderness of unsupported chords. The study provides a detailed evaluation of how these parameters influence the structural performance of battered columns, offering valuable insights for design optimization and performance assessment.

Keywords- Finite element numerical simulation; battered columns; back-to-back lipped channels; ABAQUS; Steel Built-up c-channel column; Buckling; (CFS) Cold-formed steel column; Axial Load-bearing capacity; Direct Strength Method (DSM) ;Distortional Buckling; Local Buckling

I. INTRODUCTION

The finite element (FE) method is widely regarded by engineers as a crucial tool for parametric studies, particularly in modelling cold-formed structural members. Numerous studies have employed multi-point constraints (MPC) in ABAQUS to simulate fasteners connecting cold-formed steel (CFS) elements [1, 2, 3, 4]. Due to their high axial strength, built-up columns are frequently used in construction to enhance structural efficiency. Fasteners such as bolts, screws, welds, and rivets are employed to join individual CFS sections, forming built-up sections that serve as primary load-bearing components. These built-up sections can achieve greater axial compression capacity than separate channel sections when composite action occurs. Self-drilling screws, in particular, are advantageous as they reduce labour time and eliminate the need for pre-drilling. Extensive research has explored the buckling behaviour of axially loaded CFS components. Chen et al. [5] conducted experimental studies to assess various buckling modes of CFS-lipped channel members, focusing on local-distortional buckling and its impact on post-buckling behaviour and ultimate strength. Roy et al. [6] examined built-up

steel columns with varying back-to-back distances between sections under axial loads. They found that increasing the vertical distance between connecting channels reduced the columns' load-bearing capacity, especially in medium and slender columns compared to stout and short columns. Roy et al. [7] performed experimental and analytical studies on self-drilling screw connections fastened built-up columns, developing equations to predict their reduced axial strength. El-Aghoury et al. [8] investigated box-section batten columns made of four angles connected by batten plates. They analyzed different column lengths and slenderness ratios ($\lambda_{\text{chord}}/\lambda$ values of 0.67, 1.67, and 2.6) and recommended maintaining $\lambda_{\text{chord}}/\lambda \leq 0.5$, not exceeding 0.75 for back-to-back CFS components. Anbarasu [9] experimentally studied CFS-lipped four-angle batten columns with varying lengths and slenderness ratios (λ ranging from 20 to 40, and $\lambda_{\text{chord}}/\lambda$ between 0.35 and 0.64). The study concluded that the $\lambda_{\text{chord}}/\lambda$ ratio significantly influenced column performance, recommending lower values. The research also found that capacity predictions from NAS [10] and EC3 [11] were conservative. Kherbouche et al. [12] demonstrated the superior performance of closed built-up CFS sectional configurations. Dar et al. [13] conducted numerical investigations on CFS batten columns with two channels, evaluating the impact of changes in λ_{section} (30 and 80) and λ (20 to 180). They found that strength estimates for short columns were overly optimistic based on NAS [10] and EC3 [11]. Vijayanand and Anbarasu [14,15] carried out numerical studies on lipped channel CFS batten columns and developed design guidelines, though only limited parameters were examined. This study employs finite element modelling (FEM) to simulate the behaviour of batten columns constructed from double-lipped C-channel sections, forming built-up open cold-formed steel (CFS) configurations joined with self-drilling screws. These built-up sections exhibit significant potential for superior load-bearing capacity compared to conventional single-section components. To validate the developed FEM, its results were compared against experimental test data from the literature on batten columns made of built-up CFS sections. Upon validation, the FEM was employed in a parametric analysis of built-up cold-formed steel (BCFS) batten columns. Based on the numerical findings, the study proposes enhanced design guidelines to investigate the influence of key parameters on structural behaviour, such as back-to-back spacing and slenderness ratio, along with other sectional dimensions. These guidelines aim to ensure accurate and reliable

predictions for the load-carrying capacity and failure modes of CFS batten columns.

II. FE Model investigation

A. General description

A non-linear finite element using ABAQUS [2] was employed to create a numerical model that simulates the behavior of a cold-formed steel batten column, incorporating both its elastic and plastic responses. This model aims to develop a dependable simulation of the behavior of batten columns made from built-up cold-formed steel (BCFS).

The following analysis section delineates the model's geometry and the material properties.

Buckling analysis using finite element methods necessitates two phases of evaluation. The initial phase entails identifying the analysis of the columns' buckling modes of shapes by Eigenvalue. The elastic linear analysis utilizes the (*BUCKLE) command from the library of the ABAQUS, with the applied load during a designated step. This analysis evaluates multiple buckling modes, from which the most pertinent mode identified by the Eigenvalue analysis is chosen. The second stage involves a nonlinear load-displacement analysis considering initial imperfections and nonlinearity of the material. This thorough analysis identifies the columns' ultimate capacity, strains, axial shortenings, failure modes of shape and lateral displacement.

B. Finite element mesh and materials modeling

For simulation, each detailing of the cold-formed section included end-loading plates, batten plates, and CFS channels in the ABAQUS finite element program using the S4R shell element from the ABAQUS library.

Every node within this shell element in the ABAQUS program has 6 degrees of freedom and is used in various fields. Modelling the lower and upper-end plates was accomplished with a refined mesh of three-dimensional four-node bilinear rigid quadrilateral shell elements (R3D4) from the library of ABAQUS elements.

Convergence methodologies studies were conducted to identify the optimal mesh that ensures sufficient accuracy while minimizing computational time modeling cold-formed steel built-up section batten columns. A fine mesh size of 5×5 mm as (length \times width) yielded satisfactory accuracy in modeling the built-up section columns, with a finer mesh employed at the corners as illustrated in Fig. 1. A reference point was established at a perpendicular distance from the plane of each end plate, orientated towards the center of the plate, as depicted in Fig. 1.

The reference points delineate the effective length of each specimen between the two articulated supports. The boundary conditions were applied to the RPs, while the load was designated to the RP of the upper-end plate. The top loading plate is modeled for the cold-formed steel C-channels using a "Tie" constraint in ABAQUS during the loading method. This command ensures that the rotations and displacements of the linked parts stay constant throughout the loading process. The tie constraint can be employed in ABAQUS [2] to connect three-dimensional shell meshes with other three-dimensional shell meshes automatically. The stress and strain relationship is simplified and approximated as bilinear or idealized finite element analysis. This approximation is applied to the cross-section. With its versatile capabilities, ABAQUS allows for using a multilinear stress-strain curve, demonstrating its adaptability to handling various material behaviors. This parametric study examined carbon steel properties. Steel is modeled as von mises isotropic hardening, with a minimum yield (F_y) of 355 MPa and an ultimate strength (F_u) of 510 MPa. We used 81000 MPa for shear modulus. Steel is simulated using the bilinear elastic-plastic stress-strain curve. The linear elastic part of the curve used Young's modulus of $E_o = 210$ GPa and Poisson's ratio of 0.3. The nonlinear analysis of the model expands isotropically with plastic hardening from a Von Mises-criterion-isotropic yield surface.

C. loads and Boundary conditions fastener and contact modelling

A finite element analysis employing the ABAQUS software program was developed to simulate the behavior of pin-ended built-up columns with cold-formed sections.

Figure 1 demonstrates the implementation of displacements and rotations (boundary conditions) at the upper and lower reference points (RPs) to replicate the pin-ended supports.

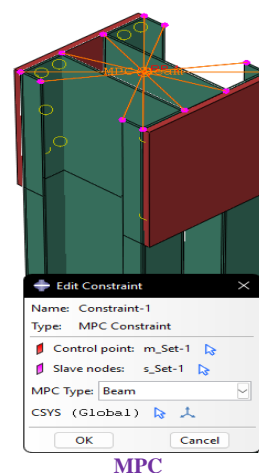
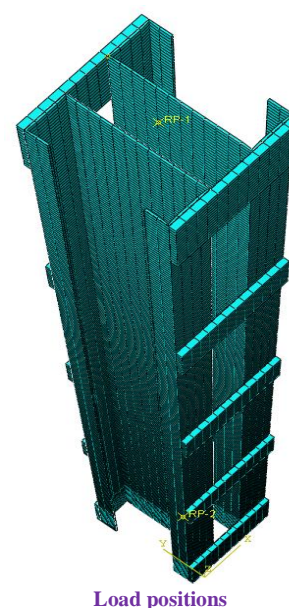
The CONN3D2 element is characterized as a three-dimensional beam connector featuring two nodes and six degrees of freedom per node were employed to represent the self-drilling screws [16,17, 18], as illustrated in Figure 1

The analysis procedure mirrored methodologies used in comparable prior studies [22]. The columns were prevented from being translated in the X- and Y-directions and from rotating in the Z-axis in the upper point of the columns.

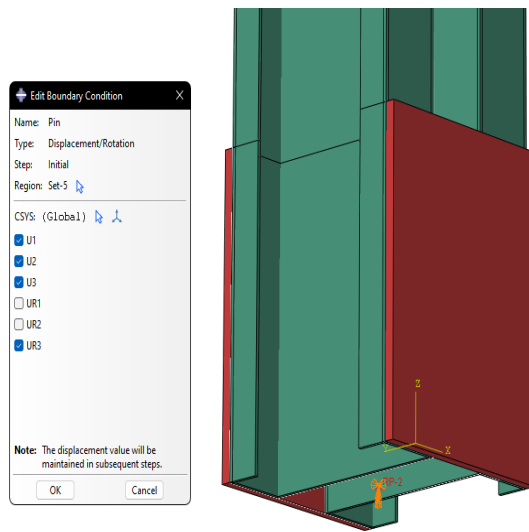
The column end conditions were constrained against translations in the X, Y, and Z axis and rotation

in the Z direction, as illustrated in Figure 2.

A load was applied to the force at the end plate RP. In order to apply the load in stages, a modified version of the RIKS technique found in the ABAQUS [2] library was utilized. This column examination under axial compressive force (p_u) employs the specified loading and boundary conditions.

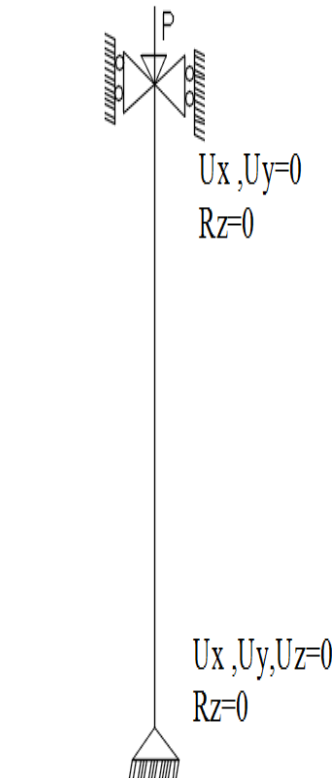
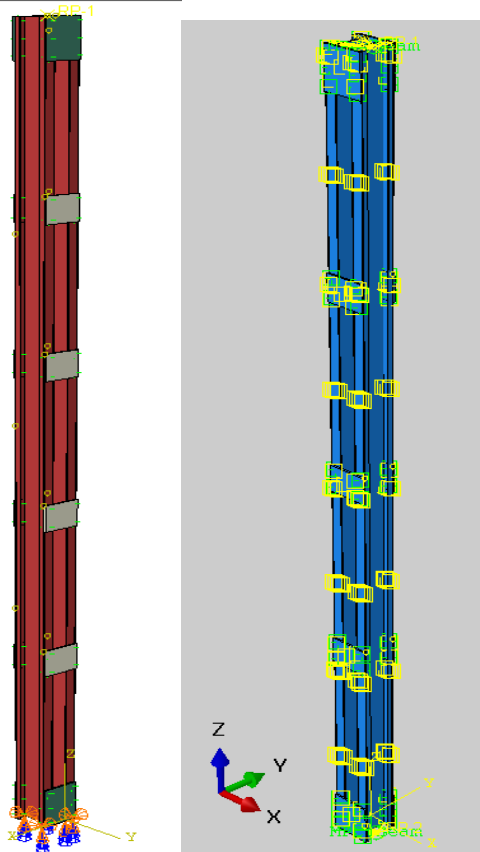


MPC



Boundary conditions meshing

a) Finite elements mesh, load application, and Boundary condition



b) Interconnector bolts & arrangement of bolts
Figure1. Numerical modeling a) Finite elements mesh, load application, and Boundary condition b) arrangement of bolts

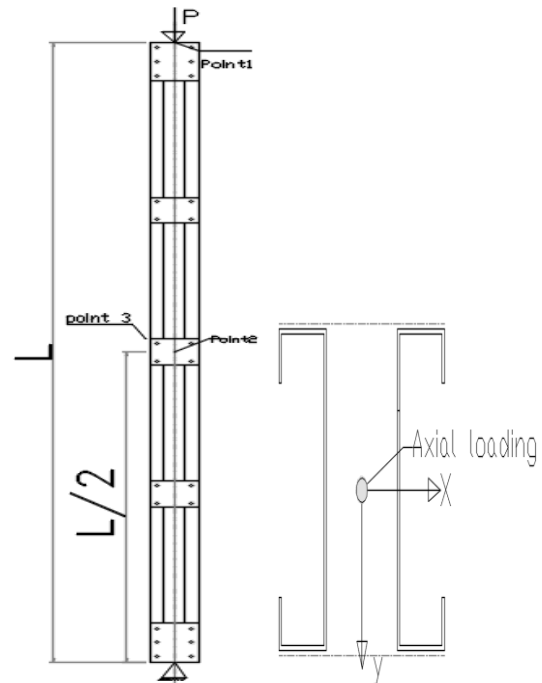


Figure2. Loading positions at column upper loaded end and support position at column lower support end for column subjected to axial and Uni-axial loads.

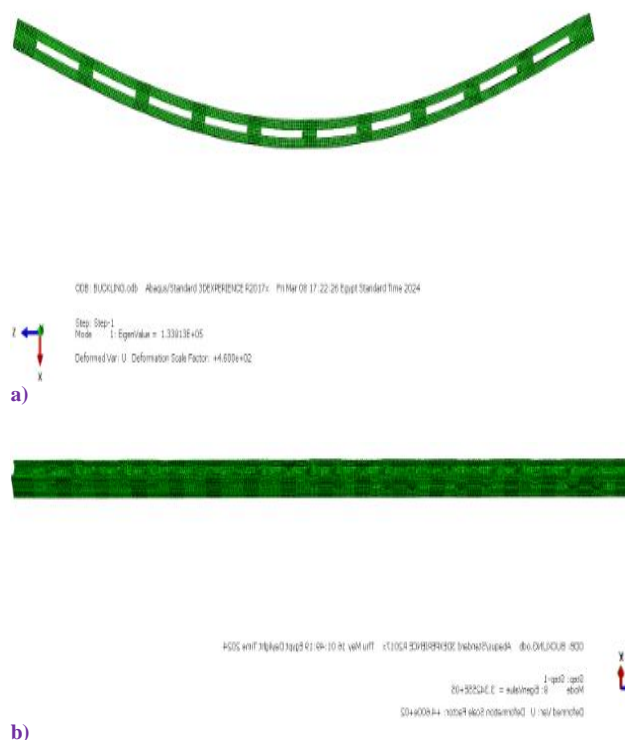


Figure3. Initial geometric imperfection modes (Eigen mode 1) for a 4.6m built-up column.
(a) Overall buckling and (b) Local buckling.

D. Initial geometric imperfections

The analyzed finite elements consider the observed magnitudes of both failure modes: local buckling and overall buckling.

Eigenvalue analyses of the column can be performed to ascertain the buckling modes and delineate the overall imperfections. The literature review [20] indicates that the average overall imperfections for the tested specimens were determined to be 1/1000 of the total length of the specimen. Imperfections were simulated in battened columns fabricated from assembled cold-formed steel sections. All buckling modes forecasted by the ABAQUS [2] Eigenvalue analysis are standardized to 1.0. Moreover, the value of the overall geometric and initial local imperfections was measured in the buckling modes, as seen in Figure 3.

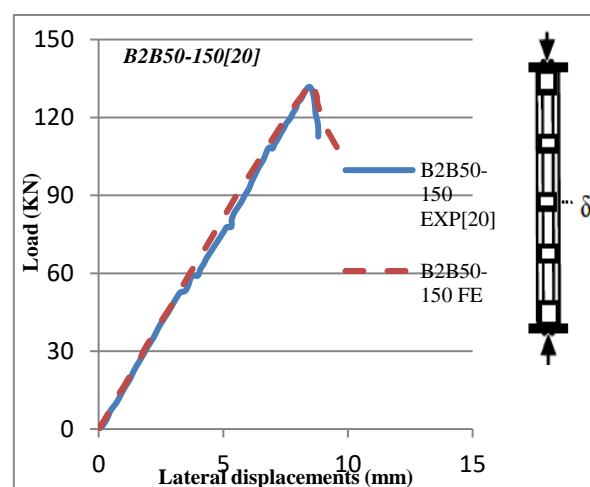
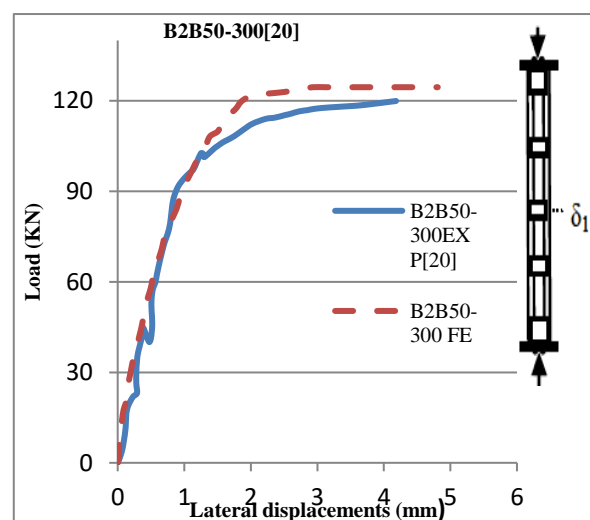
E. Verification of the developed Finite Element Model

To evaluate the accuracy of the finite element model using ABAQUS [2] in simulating the actual behavior of CFS material, the outcomes of three experimental tests documented in Dabaon [20] conducted experimentally cold-formed built-up C sections,

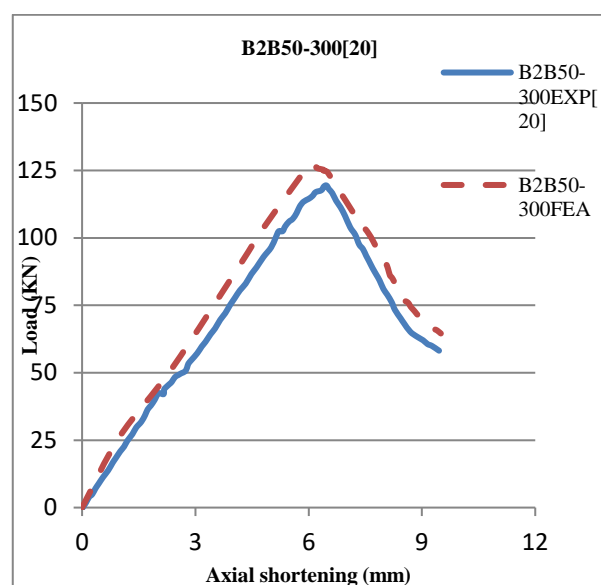
indicating that all factors, including the overall slenderness ratio λ ranging from (50 to 110) and the factor $\lambda_{\text{chord}}/\lambda$, influenced the performance of battened columns, which were compared with the outcomes of the present finite element model.

The correlations among deformed shape, load vs lateral displacement, and load versus axial shortening were analyzed compared to the test results, as shown in Fig. 4. Table 1 demonstrates a satisfactory correlation between the experimental ultimate loads and the corresponding values of the current finite element model.

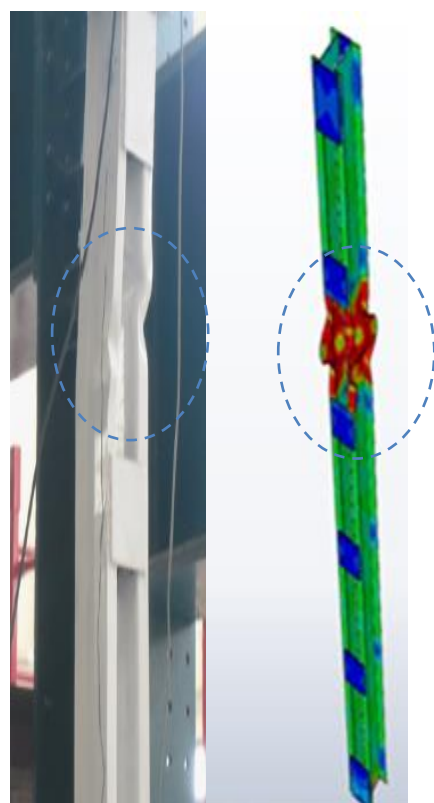
The analysis of the Finite Element Analysis (FEA) results in conjunction with the experimental outcomes across all four dimensions specifically peak strength, failure mode, axial shortening, and the load versus displacement relationship reveals a significant correlation. As a result, the finite element model is well-suited for the proposed parametric studies.



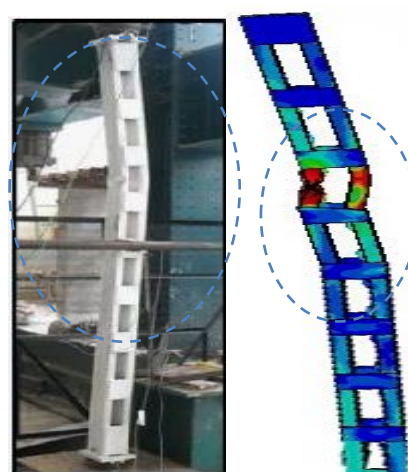
A) Lateral displacement-load relationships



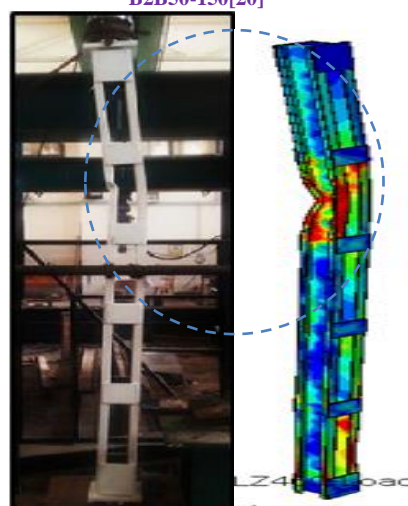
B) Axial shortening -load relationships



B2B50-300 [20]



B2B50-150[20]



B2B75-300[20]

C) Mode of failure comparison between test specimens and the finite model of [20].

Fig. 4. (A): Lateral displacement-load relationships, (B): Axial shortening, and (C): failure modes Flexural buckling (FB) and local buckling (LB)

Table1. Comparison of the strengths of battened column specimens in FEA and in the experimental test [20].

Specimen	Ptest (KN) (Exp)	mode of failure (Exp)	P F.E.A (kN)	Failure mode	Ptest/ PF.E.A
B2B50-300	119.11	FB+LB	123	FB+LB	0.96
B2B75-300	125.2	LB	126.5	LB	0.98
B2B50-150	133.12	FB	134	FB	0.99
Mean					0.98
COV					0.01

F. Parametric study

The parametric study analyzed columns with varying back-to-back distances between the two channels (B1) and different buckling lengths (L_z), as shown in Figure 5. A total of 36 columns were evaluated, with dimensions depicted in Figure 5 and listed in Table 2. The column lengths were 2400 mm, 3000 mm, 4600 mm, and 5800 mm, classified into four series based on back-to-back distances (B1) of 40 mm, 60 mm, 80 mm, and 90 mm.

Each column was subjected to axial loading. The buckling lengths (L_z) of single channels within each series were 600 mm, 460 mm, 450 mm, 340 mm, 250 mm, and 175 mm, corresponding to slenderness ratios between batten plates (λ_z) of 38.7, 29.67, 29.03, 21.93, 16.12, and 11.29, respectively. According to AISI S-100:2016 [10], the overall slenderness ratios ($\lambda = L/r_{min}$) ranged from 50 to 162. Specimen label designations are illustrated in Figure 6.

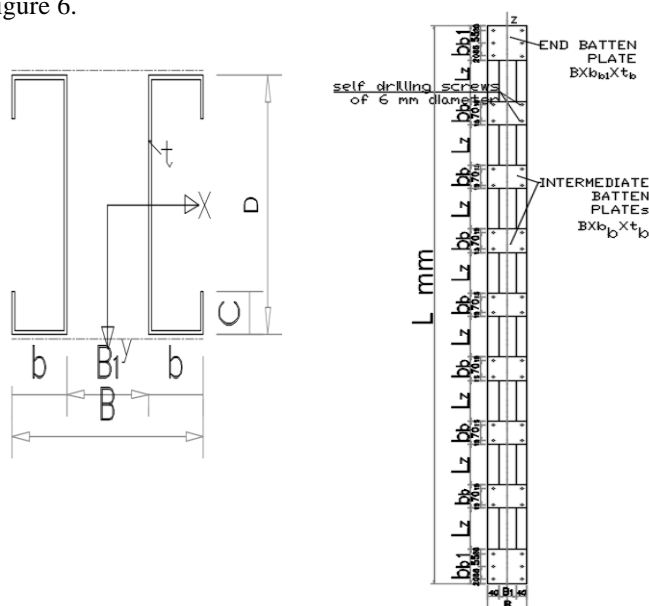


Fig.5.The cross-sectional dimensions analyzed in the parametric study.

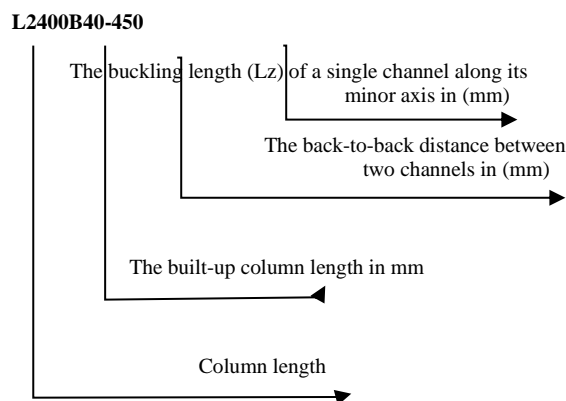


Fig 6. Label designations of the specimen

Table 2. The parametric study's specimen dimensions:

Series	Specimen	L (mm)	Lz (mm)	B1/D	λ_z	$\lambda = L/r_{min}$	Channel cross-section in (mm) $D \times b \times c \times t$	Batten plates' dimensions in (mm)		
								bb	bb1	tb
B40	L2400B40-450	2400	450	0.33	29.03	71.29	$120 \times 40 \times 20 \times 2$	100	150	6
	L2400B40-340	2400	340	0.33	21.93	68.71	$120 \times 40 \times 20 \times 2$	100	150	6
	L2400B40-175	2400	175	0.33	11.29	66.08	$120 \times 40 \times 20 \times 2$	100	150	6
	L3000B40-600	3000	600	0.33	38.71	90.20	$120 \times 40 \times 20 \times 2$	100	150	6

	L3000B40-460	3000	460	0.33	29.67	86.60	120 × 40 × 20×2	100	150	6
	L3000B40-250	3000	250	0.33	16.12	82.90	120 × 40 × 20×2	100	150	6
	L4600B40-450	4600	450	0.33	29.03	128.13	120 × 40 × 20×2	100	150	6
	L4600B40-340	4600	340	0.33	21.93	126.70	120 × 40 × 20×2	100	150	6
	L4600B40-175	4600	175	0.33	11.29	125.30	120 × 40 × 20×2	100	150	6
	L5800B40-600	5800	600	0.33	38.71	162.10	120 × 40 × 20×2	100	150	6
	L5800B40-460	5800	460	0.33	29.67	160.13	120 × 40 × 20×2	100	150	6
	L5800B40-250	5800	250	0.33	16.12	158.18	120 × 40 × 20×2	100	150	6
B60	L2400B60-450	2400	450	0.5	29.03	59.60	120 × 40 × 20×2	100	150	6
	L2400B60-340	2400	340	0.5	21.93	56.49	120 × 40 × 20×2	100	150	6
	L2400B60-175	2400	175	0.5	11.29	53.27	120 × 40 × 20×2	100	150	6
	L3000B60-600	3000	600	0.5	38.71	75.70	120 × 40 × 20×2	100	150	6
	L3000B60-460	3000	460	0.5	29.67	71.50	120 × 40 × 20×2	100	150	6
	L3000B60-250	3000	250	0.5	16.12	67.10	120 × 40 × 20×2	100	150	6
	L4600B60-450	4600	450	0.5	29.03	103.92	120 × 40 × 20×2	100	150	6
	L4600B60-340	4600	340	0.5	21.93	102.16	120 × 40 × 20×2	100	150	6
	L4600B60-175	4600	175	0.5	11.29	100.40	120 × 40 × 20×2	100	150	6
	L5800B60-600	5800	600	0.5	38.71	131.6	120 × 40 × 20×2	100	150	6
	L5800B60-460	5800	460	0.5	29.67	129.26	120 × 40 × 20×2	100	150	6
	L5800B60-250	5800	250	0.5	16.12	126.84	120 × 40 × 20×2	100	150	6
B80	L2400B80-450	2400	450	0.67	29.03	51.99	120 × 40 × 20×2	100	150	6
	L2400B80-340	2400	340	0.67	21.93	51.94	120 × 40 × 20×2	100	150	6
	L2400B80-175	2400	175	0.67	11.29	51.94	120 × 40 × 20×2	100	150	6
	L4600B80-450	4600	450	0.67	29.03	99.56	120 × 40 × 20×2	100	150	6
	L4600B80-340	4600	340	0.67	21.93	99.56	120 × 40 × 20×2	100	150	6
	L4600B80-175	4600	175	0.67	11.29	99.56	120 × 40 × 20×2	100	150	6
B90	L2400B90-450	2400	450	0.75	29.03	51.94	120 × 40 × 20×2	100	150	6
	L2400B90-340	2400	340	0.75	21.93	51.94	120 × 40 × 20×2	100	150	6
	L2400B90-175	2400	175	0.75	11.29	51.94	120 × 40 × 20×2	100	150	6
	L4600B90-450	4600	450	0.75	29.03	99.56	120 × 40 × 20×2	100	150	6
	L4600B90-340	4600	340	0.75	21.93	99.56	120 × 40 × 20×2	100	150	6
	L4600B90-175	4600	175	0.75	11.29	99.56	120 × 40 × 20×2	100	150	6

the precision and reliability of our findings.

The ultimate strengths (PFE), failure modes, and non-dimensional critical slenderness (λ_c) and ($\bar{\lambda}$) of the column, as established by the North American Specification [10] and euro code[11], respectively, are presented in Table 3. Also, the overall slenderness ratio of the column (λ) = L/i min considering the modified length in [10] is listed in Table 2. The relation between (λ_z) and (λ) studied in this paper is shown in Fig 7.

The results of this parametric research were obtained via the examination of the battened columns finite element model for built-up steel sections. Applying this comprehensive methodology ensures

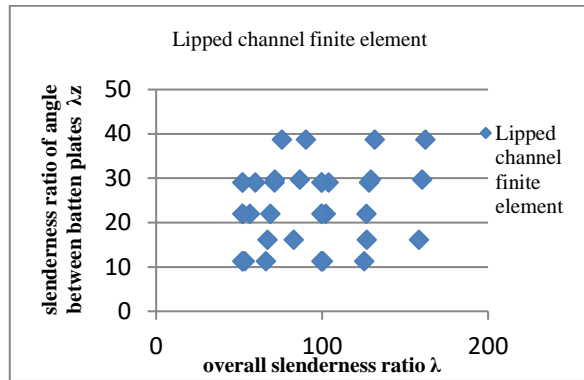


Fig.7. Critical parameters (λ_z and λ) were examined in the study for CFS battened columns made of channels.

III. Design rules for built-up columns

A. Design rules according to North American (AISI S-100:2016) [10]

The design code NAS [10] introduces different designs methodologies: the effective width (EWM) and direct strength (DSM) methods and Estimating the elastic critical buckling stress is the primary factor determining the accuracy of DSM. Battened columns are non-prismatic, making elastic critical buckling stress quantification difficult.

Global buckling and yielding

Global buckling and yielding refer to the failure modes of a structural element under the combined effects of flexural, torsional loads, and flexural-torsional.

$$P_{ne} = A_g F_n \quad (1)$$

The global compressive stress, F_n , is calculated by the following equation:

$$\begin{cases} F_n = (0.658^{\lambda_c}) f_y & \text{for } \lambda_c \leq 1.5 \\ F_n = \left(\frac{0.877}{\lambda_c^2}\right) f_y & \text{for } \lambda_c > 1.5 \end{cases} \quad (2)$$

$$F_{cre} = \frac{\pi^2 E}{(KL/r)^2} \quad (3)$$

The AISI (λ_c) non-dimensional slenderness ratio is calculated as $\lambda_c = \sqrt{(F_y / F_{cre})}$,

F_{cre} denotes the least elastic global buckling stresses pertinent to different modes of shape, such as torsional, flexural, and flexural-torsional.

The symbol (r) indicates the full cross-section radius of gyration about the buckling axis.

$$\lambda_{mod} = \sqrt{\left(\frac{kl}{r}\right)_o^2 + (\lambda_{chord})^2} \quad (4)$$

where:

λ_{mod} : the built-up columns modified slenderness ratio

$\frac{kl}{r}$: the column's slenderness ratio of the whole cross-section

λ_{chord} : $\frac{L_z}{r_i}$ is the slenderness ratio of the chord

Local buckling in conjunction with global buckling and yielding

"effective width method"

$$P_{nl} = A_e F_n \quad (5)$$

Calculation of the effective width of each columns can be used to determine A_e .

$$\begin{cases} be = b & \text{where } \lambda_1 \leq 0.673 \\ be = b / \lambda_1 (1 - 0.22 / \lambda_1) & \text{where } \lambda_1 > 0.673 \end{cases} \quad (6)$$

The slenderness factor, λ_1 , is defined as $\sqrt{(f_n / f_{cr1})}$.

$$F_{cr1} = \frac{\pi^2 E}{(12(1-\nu^2)) \frac{t^2}{b}} \quad (7)$$

"The "direct strength method" is defined in AISI-S100-2016.

$$\begin{cases} P_{nl} = P_{ne} = A_g F_n & \text{for } \lambda_1 \leq 0.776 \\ P_{nl} = [1 - 0.15 (P_{cr1} / P_{ne}) 0.4] (P_{cr1} / P_{ne}) 0.4 P_{ne} & \text{for } \lambda_1 > 0.776 \end{cases} \quad (8)$$

Buckling due to distortion

$$\begin{cases} P_y = P_{nd} = A_g F_y & \text{when } \lambda_d \leq 0.561 \\ P_{nd} = [1 - 0.25 (P_{crd} / P_y) 0.6] (P_{crd} / P_y) 0.6 P_y & \text{when } \lambda_d > 0.561 \end{cases} \quad (9)$$

$$P_{crd} = A_g f_{crd}$$

P_n AISI = the least nominal loads from (p_{ne} , p_{nl} and p_{nd})

B. Design regulations according to Eurocode 3, EN 1993-1-3:2006.

The Euro code (EN 1993-1-

1:2006) [11] uses the technique of the effective width of the studied columns for the calculation of the built-up columns' un-factored design strength (PEC3) using the formulae shown below: The class 4 un-factored strength is determined by EC3 (BS EN1993-1-3) as follows:

$$PEC3 = \chi \frac{A_g F_y}{\gamma_{m1}} \quad (\text{For Class 1, 2 or 3}) \quad (10)$$

$$= \chi \frac{A_e F_y}{\gamma_{m1}} \quad (\text{For Class 4})$$

A_e and A_g denote the effective and gross area of the cross-sectional, respectively, defined in euro code [11] sections class 1, 2, 3 or 4.

F_y represents the yield stress, whereas χ is the reduction factor, which may be computed using Equation (11).

$$\chi = \left(1 / \left(\varphi + \sqrt{\varphi^2 - \bar{\lambda}^2} \right) \right) \text{ but } \chi \leq 1.0 \quad (11)$$

$$\varphi = 0.5 \left[1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2 \right] \quad (12)$$

The euro code non-dimensional slenderness ratio was calculated as follows:

$$\bar{\lambda} = \sqrt{\frac{A_g F_y}{N_{cr}}} \quad (\text{For Class 1, 2 or 3}) \quad (13)$$

$$\bar{\lambda} = \sqrt{\frac{A_e F_y}{N_{cr}}} \quad (\text{For Class 4}) \quad (14)$$

$$\bar{\lambda} = (L_{cr}/i) \cdot \left(\frac{A_e}{A_g} \right) / \lambda_1 \quad (15)$$

$$N_{cr,t} = \left(1 / i_o^2 \right) \left[G I_t + \pi^2 E I_w / L_T^2 \right] \quad (16)$$

where

$N_{cr,t}$ the section torsional buckling capacity

I_w : is the constant of warping; L_T : the constant of torsional, and L_T is the effective length of the torsional.

G : the section shear modulus

$$\lambda_1 = \pi \sqrt{E / F_y} \quad (17)$$

$\bar{\lambda} = \text{Maximum}(\bar{\lambda}_x, \bar{\lambda}_y, \bar{\lambda}_T)$

Where:

χ : the applicable buckling mode reduction factor.

L_{cr} : the buckling length considered.

N_{cr} : refers to the critical buckling force for elastic design associated with specific buckling mode

A_e : the effective cross-sectional area.

F_y : A proof stress of 0.2% ($\sigma_{0.2}$) is the same as the yield stress.

" α " imperfection factor.

Table3. A comparison of the model's strengths and the design's strengths

Series	Specimen name	FEM Results		Different design strength				FE/Code	
		PuFE (KN)	Failure Mode	PNAS (KN)	λ_c	PEC3 (KN)	$\bar{\lambda}$	PuFE / PNAS	PuFE / PEC3
B40	L2400B40-450	237.8	L+D	233.0	0.93	232.3	0.85	1.020	1.023
	L2400B40-340	241.4	L+D	240.0	0.89	232.3	0.85	1.005	1.038
	L2400B40-175	257.8	L+D	246.0	0.86	232.3	0.85	1.048	1.109
	L3000B40-600	179.2	L+D	177.6	1.17	176.8	1.06	1.009	1.013
	L3000B40-460	188.3	L+D	186.1	1.13	176.8	1.06	1.011	1.06
	L3000B40-250	197.5	L+D	195.0	1.08	176.8	1.06	1.012	1.1170
	L4600B40-450	106.9	L+F	103.5	1.67	99.9	1.63	1.033	1.070
	L4600B40-340	110.0	L+F	106.2	1.65	99.9	1.63	1.035	1.101
	L4600B40-175	115.8	L+F	108.9	1.64	99.9	1.63	1.062	1.159
	L5800B40-600	55.5	L+F	51.1	2.12	48.7	2.05	1.087	1.139
	L5800B40-460	57.8	L+D+F	54.4	2.09	48.7	2.05	1.062	1.185
	L5800B40-250	59.0	L+F	56.8	2.07	48.7	2.05	1.037	1.210
B60	L2400B60-450	260.7	L+D	260.0	0.78	266.7	0.68	1.002	0.977
	L2400B60-340	269.3	L+D+F	267.2	0.73	266.7	0.68	1.007	1.009
	L2400B60-175	276.7	L+D+F	274.0	0.69	266.7	0.68	1.010	1.037
	L3000B60-600	218.9	L+D	217.6	0.99	205.4	0.85	1.005	1.065
	L3000B60-460	223.9	L+D	222.7	0.93	205.4	0.85	1.005	1.090
	L3000B60-250	235.6	L+D+F	233.4	0.87	205.4	0.85	1.009	1.147
	L4600B60-450	155.5	L+F	154.8	1.36	142.4	1.30	1.004	1.092
	L4600B60-340	161.5	L+F	158.9	1.33	142.4	1.30	1.016	1.134
	L4600B60-175	170.3	L+D+F	163.0	1.31	142.4	1.30	1.044	1.196

	L5800B60-600	70.9	L+F	66.9	1.72	60.5	1.64	1.058	1.170
	L5800B60-460	75.0	L+D+F	72.3	1.69	60.5	1.64	1.038	1.239
	L5800B60-250	77.8	L+F	76.9	1.66	60.5	1.64	1.011	1.285
B80	L2400B80-450	277.6	L+D	276.7	0.68	267.0	0.67	1.003	1.039
	L2400B80-340	286.3	L+D	284.0	0.63	267.0	0.67	1.008	1.072
	L2400B80-175	290.6	F+D	276.8	0.67	267.0	0.67	1.050	1.088
	L4600B80-450	167.0	L+F	156.1	1.30	142.8	1.30	1.069	1.169
	L4600B80-340	169.8	L+F	159.2	1.30	142.8	1.30	1.066	1.189
	L4600B80-175	174.3	L+F	164.1	1.30	142.8	1.30	1.062	1.220
B90	L2400B90-450	285.0	L+D	276.8	0.679	267.0	0.67	1.029	1.067
	L2400B90-340	290.6	F+D	276.8	0.679	267.0	0.67	1.049	1.088
	L2400B90-175	296.7	L+D+F	276.8	0.67	267.0	0.67	1.072	1.111
	L4600B90-450	168.9	L+D+F	157.1	1.30	142.8	1.30	1.075	1.182
	L4600B90-340	171.4	L+D+F	159.4	1.30	142.8	1.30	1.075	1.200
	L4600B90-175	176.1	L+D+F	165.1	1.30	142.8	1.30	1.066	1.233
Mean Pm = Average of the array (PFEM/Pcode)								1.035	1.120
Standard deviation								0.026	0.074
Reliability index, β								3.050	3.41
Resistance factor, Φ								0.850	0.850

L: local buckling

D; distortion buckling

F: flexural buckling

The results obtained from the analysis of the finite element of the examined (CFS) battened columns are shown in Table 3, which also compared the findings with different analytical computations from many codes. The results indicate that the examined built-up columns with nondimensional slenderness (λ_c) < 0.6 mainly exhibited failure modes distortional (D) and local buckling (L). Conversely, sections with nondimensional slenderness (λ_c) > 1 mostly experienced failure owing to a mix of local buckling (L) and overall flexural buckling (F) failure modes.

IV. Reliability analysis

The reliability analysis following ASCE Specification [21], aiming for a reliability index (β) of 2.5, as recommended for cold-formed steel (CFS) structural members.

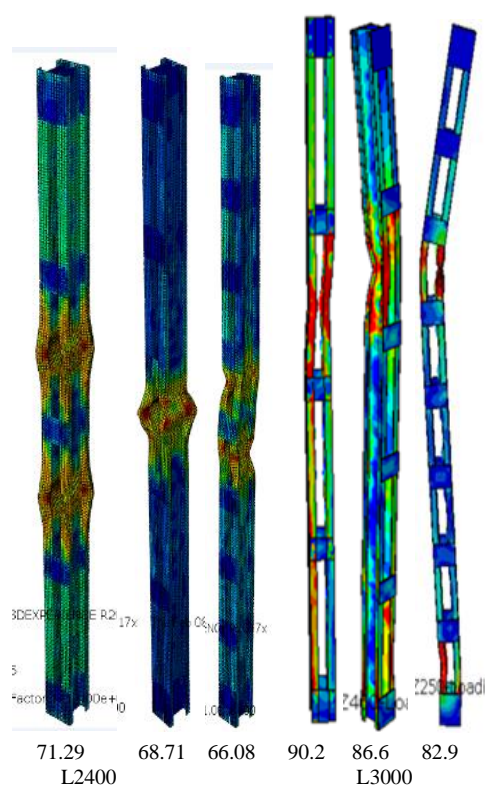
The reliability index (β) was calculated using the load combination 1.2DL + 1.6LL for concentrically loaded compression members, where DL and LL represent dead and live loads, respectively. A capacity reduction factor (ϕ) of 0.85 was applied per NAS [10] and EC3 [11], with a DL/LL ratio of 0.2. Statistical parameters for the analysis included $M_m = 1.10$, $F_m = 1.00$, $V_m = 0.10$, and $V_F = 0.05$, as specified by ASCE [21]. A correction factor (C_p) was applied to account for the influence of data point quantity on the reliability index, as recommended by

NAS [10]. A reliability index above 2.5 indicates a dependable design process, with higher values reflecting greater prediction accuracy. The analysis procedure mirrored methodologies used in comparable prior studies [22].

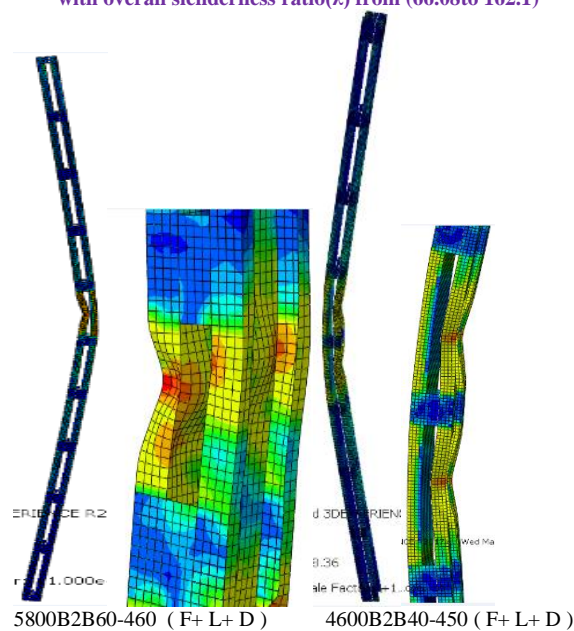
V. Discussion of the results

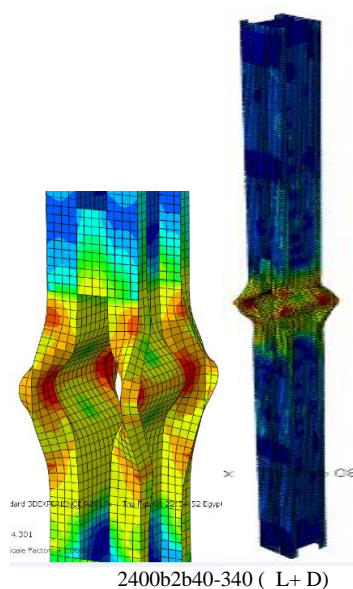
A. Failure modes' shape

For columns subjected to axial loads, three primary failure modes occur due to buckling: local buckling, flexural buckling, and distortional buckling. Table 3 summarizes the maximum load capacities and failure scenarios for each model.



(a) Non-linear FE analysis deformed shapes for series B40 with overall slenderness ratio(λ) from (66.08to 162.1)





b)
Fig.8.Failure Mode shapes

In the column model L2400B40-340, which had an ultimate load of 241.4 KN, significant waves of local buckling were observed in the web and flange at failure. The data further indicates that buckling waves appeared in a single channel when the overall slenderness ratio (λ) ranged from 90 to 162.

Notably, models L2400B60-175 and L2400B90-175 exhibited non-linear stress distribution in one channel, as depicted in Fig. 8(b), while stress in the other channel was distributed more linearly.

In contrast, for models L3000B60-340, L3000B60-175, L3000B80-175, and L3000B90-340, an interaction between flexural and distortional buckling was observed, as shown in Fig. 8(a)

In cold-formed channels, local buckling and distortion distortion buckling are similar.

Thus, a single channel between batten plates has distortion or local deformed shapes.

B. Comparison between FEA results and design Codes.

This section compares the finite element (FE) ultimate strength results with the design rules of EC3 [11] and AISI [10], as summarized in Table 3 for axial loads. Axial load capacities were determined using the practical width approach. Figures 10 and 11 illustrate the relationship between the normalized axial load ratio (P_u/P_y) and the non-dimensional slenderness ratios, λ_c for AISI [10] and $\bar{\lambda}$ for EC3 [11]. Here, P_u represents the ultimate load from the finite element analysis, and P_y is the yield load calculated as the product of the gross cross-sectional area (A_g) and yield stress (F_y) ($P_y = A_g * F_y$). The predicted ultimate loads from AISI [10] and EC3 [11] closely match the FE results, as shown in Figures 10 and 11. The reliability index (β) was maintained between 2.5 and 3.5, ensuring safe and reliable design under various loading conditions. The AISI code incorporates a modified slenderness factor to account for (L_z), as shown in Equation 4. The AISI predictions were more conservative, with safety factors ranging from 1.0028 to 1.07 for axial loads, as shown in Table 3. EC3 predictions had safety factors between 1.00982 and 1.285, showing better alignment with experimental results. The EC3 design provisions account for imperfections and effective widths, particularly for medium-battened columns, where the effects of (L_z) accumulate. The slenderness ratio between batten plates (λ_z) significantly impacts axial strength. For instance, in columns with a length of 4600 mm and an initial λ_z of 11.29, increasing λ_z to 21.9 reduced axial strength by 4%, while further increasing it to 29.03 led to a 30% reduction. Comparisons show that AISI [10] generally provides more conservative results than EC3 [11]. However, in some cases, the FE analysis and design codes yielded highly similar outcomes, as shown in Figure 7 and documented in Table 3.

A notable observation is that as the column back-to-back distance-to-depth ratio ($B1/D$) decreases, the normalized axial load ratio (P_{UFE}/P_y) also decreases across different column lengths. Additionally, for the same $B1/D$, longer columns exhibited lower P_{UFE}/P_y ratios. Overall, the AISI design code showed satisfactory agreement with the FE modeling results for axially loaded columns.

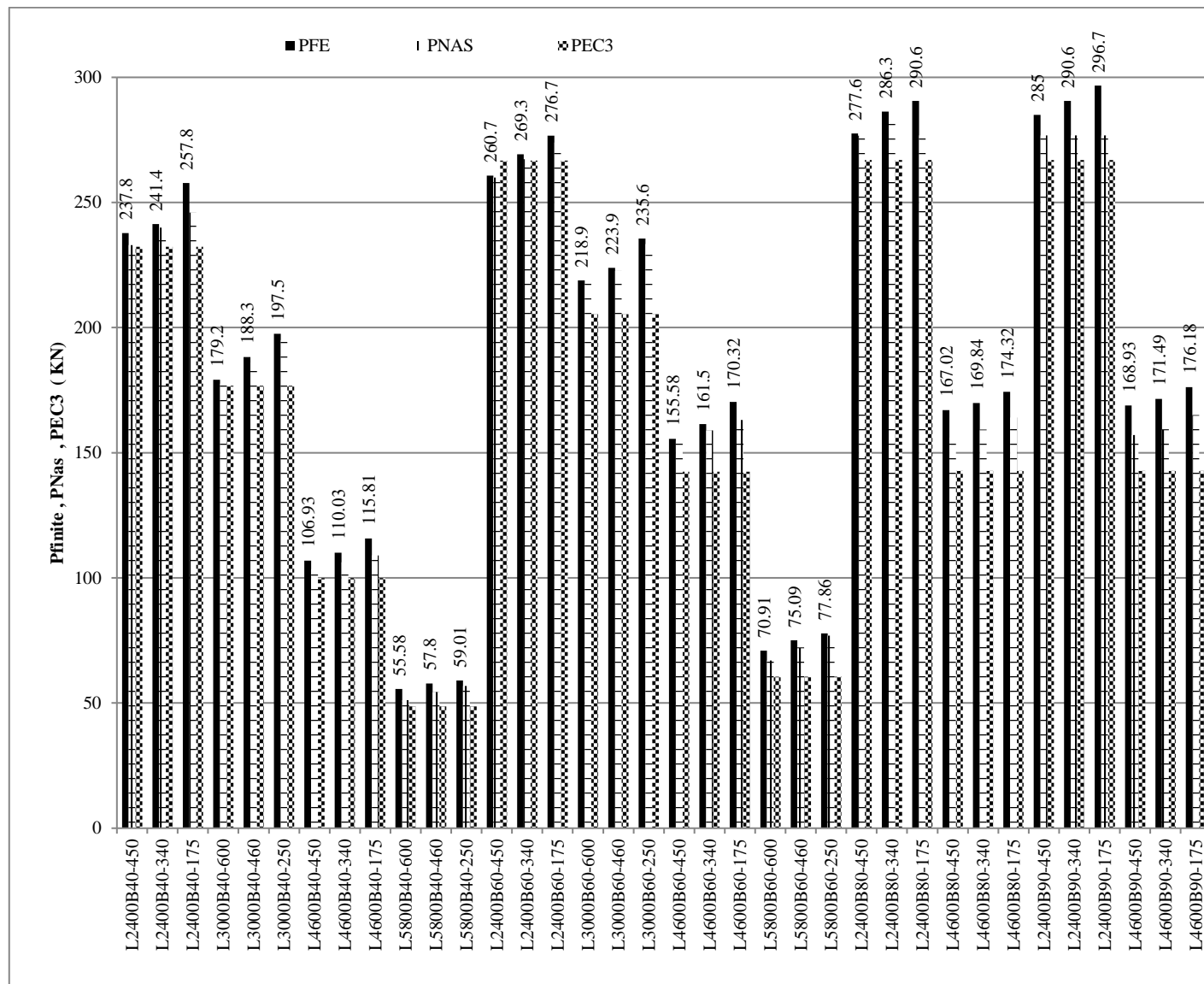
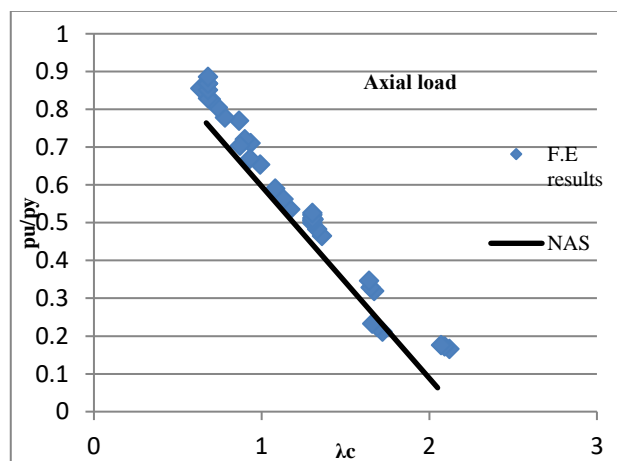
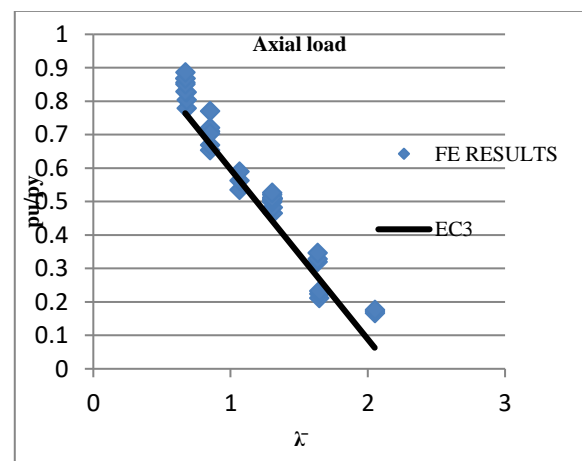


Figure 9: Comparison between results from the tests with the predictions of the design strength

Fig10. Comparison of the finite element strengths And AISI [31] design code non-dimensional (λ_c)Fig11. Comparison of the finite element and EC3 [32] design non-dimension slenderness slenderness (λ)

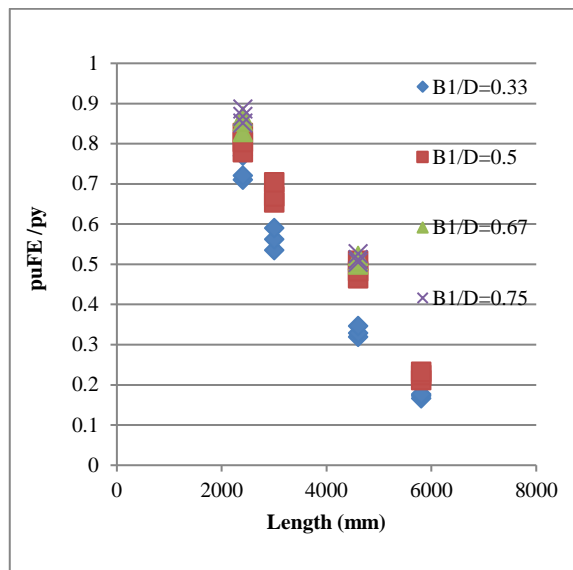


Fig12. Effect of B1/D ratio for different column lengths on the column capacity

C. Axial shortening versus axial load

The axial compression magnitude was assessed at point 1, situated at the loaded end of the column, as seen in the finite element in Figure 1.

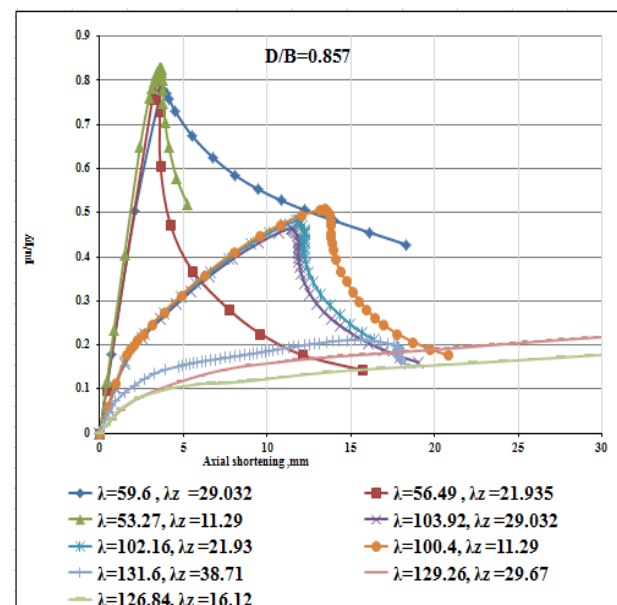
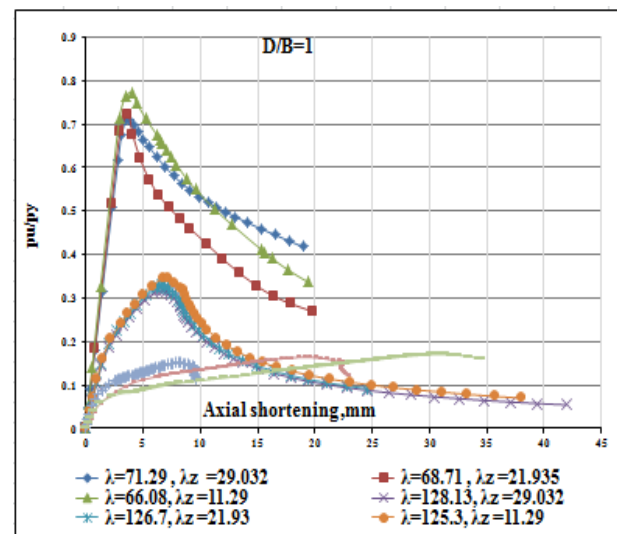
Figure 13 illustrates the CFS relationship between axial load versus axial shortening for different models.

The structure consists of columns with varying slenderness ratios of channels between batten plates and overall slenderness ratios. The figure illustrates the relationship between axial shortening and axial load response of columns with the same column depth-to-width ratio (D/B).

The maximum axial strengths of columns decrease as the overall slenderness ratio increases (λ).

Only a tiny amount of nonlinearity is seen in the plots of axial load versus axial shortening before the columns reach their maximum axial strengths. Furthermore, there is a gradual decrease in the axial strength observed in the columns after reaching their peak behavior. The columns experienced failure due to a combination of local and global (or flexural) buckling modes. The columns exhibited the failure modes identified as flexural and local buckling. When the column's depth-to-width ratio (D/B) is less than or equal to 0.75, accompanied by high overall slenderness ratios, a pronounced nonlinear response is seen in the correlation between axial load and axial shortening. For axial columns, the peak axial strength of columns and the axial shortening are influenced by the column depth-to-width ratio (D/B) for the same cross-section. For example, columns having (D/B) of 0.7058 exhibited a reduction in peak

axial strengths by 8%, 7.3% and 6.7% for $L=2400$ and $LZ=29.032$, 21.935 and 11.29 respectively, if the value of (D/B) is increased from 0.7058 to 0.857 and by 14%, 13.9 % and 11.2% if the value of (D/B) is increased from 0.75 to 1 for $LZ=450$, 340 and 175 respectively. When comparing models with the same column diameter (D/B) but different loading types, it was observed that the axially loaded column exhibited greater stiffness than the columns subjected to other loading types.



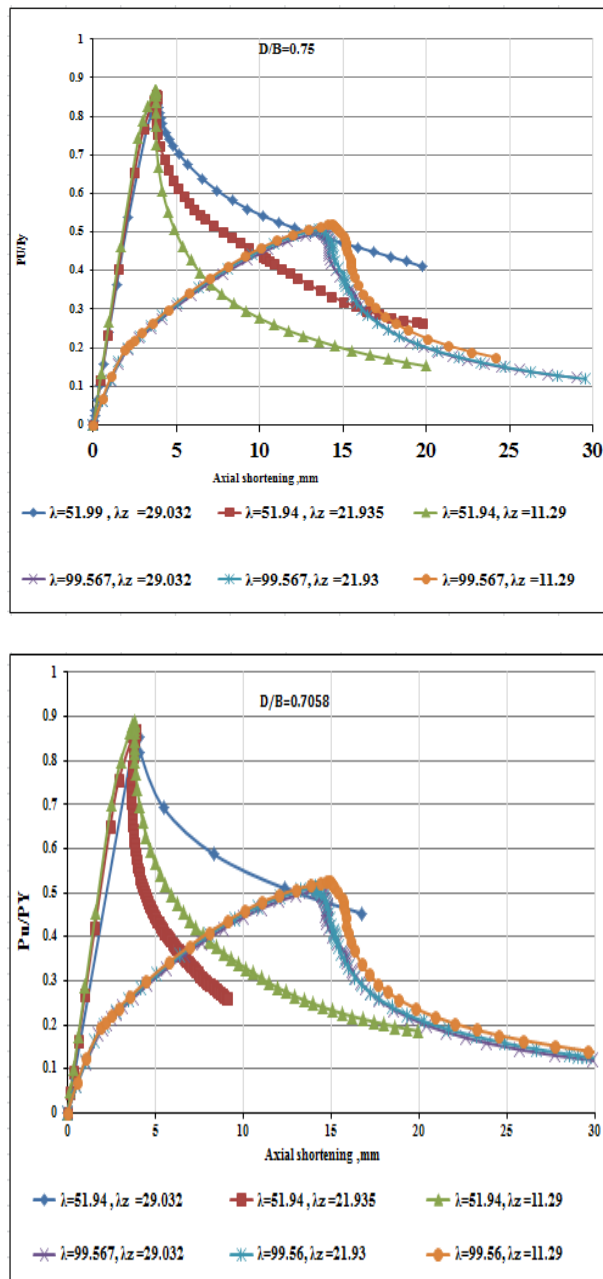


Figure13:
Relationships between load and axial shortening for axially loaded columns

D. Load and lateral displacement (U_x and U_y)

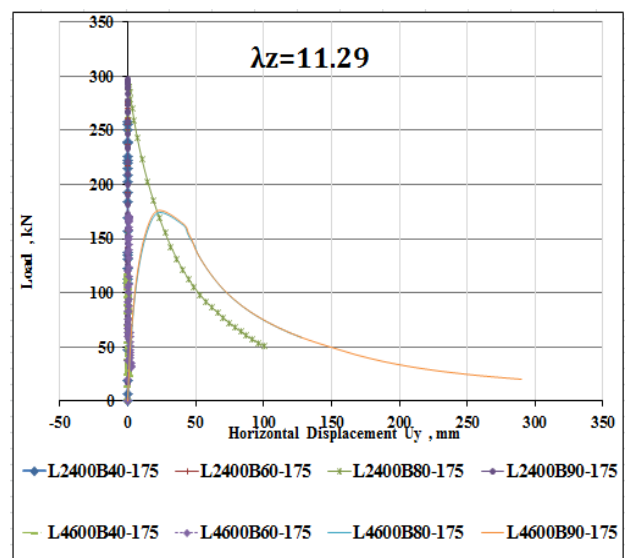
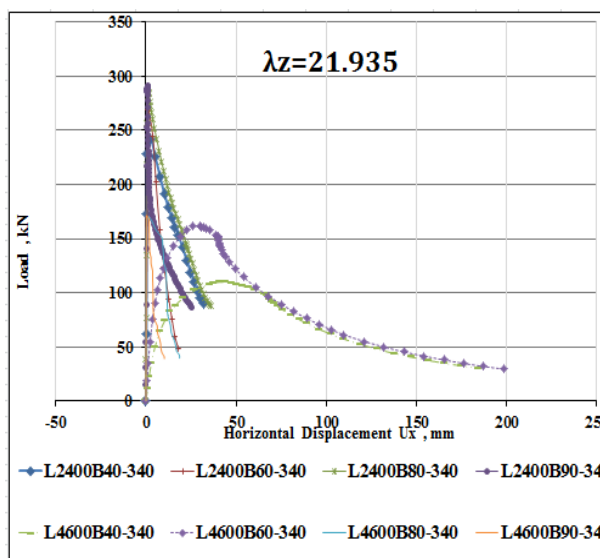
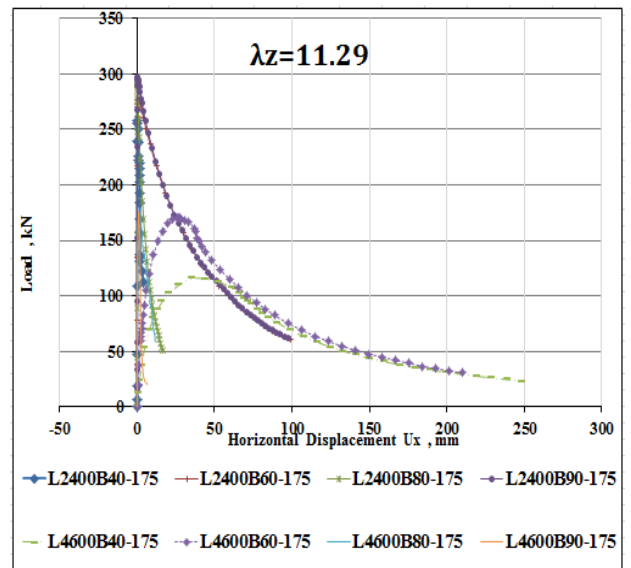
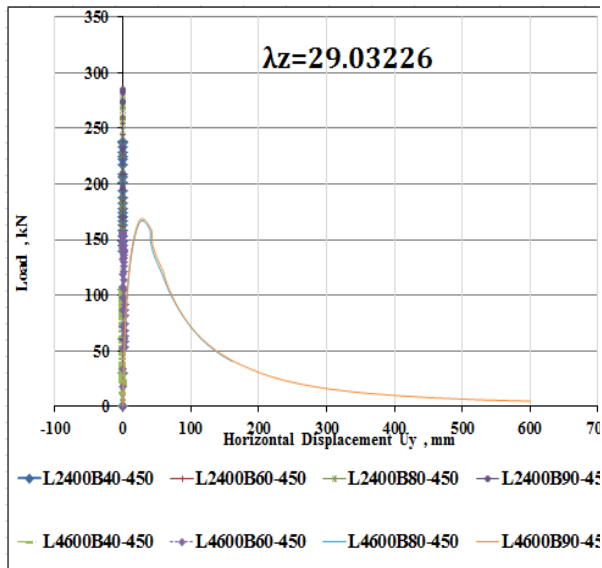
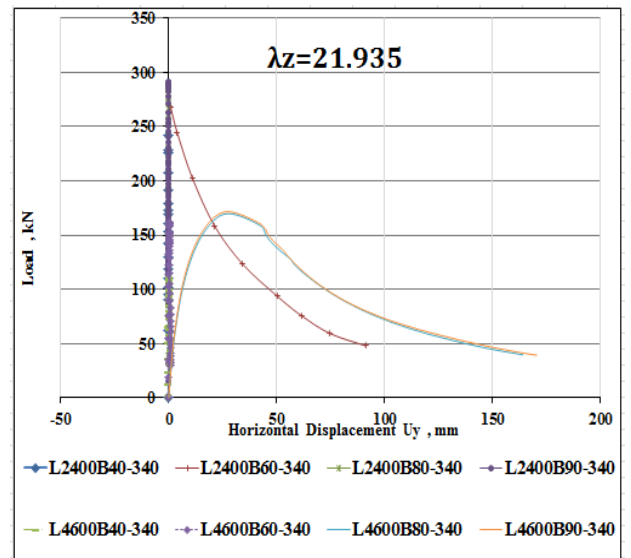
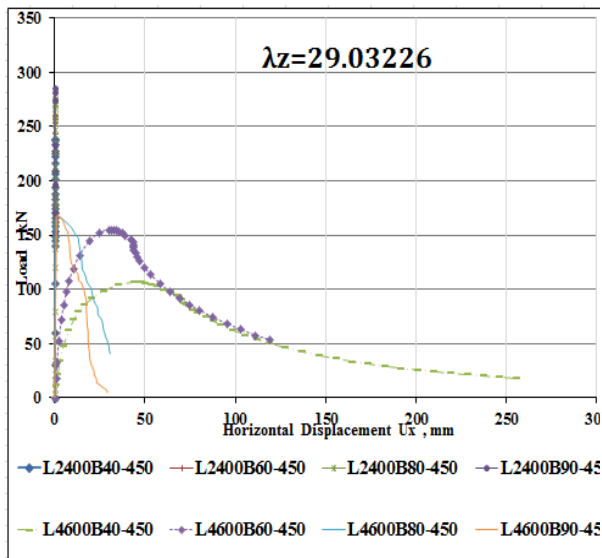
The lateral displacements were measured at two locations at the midpoint of the model to quantify the displacement in both the X and Y directions. The first location, referred to as "point2," is shown in the figure2. The second location is at the midpoint of the cross-sectional flange and is designated as point 3, as depicted in Figure 2.

In the axially loaded column, the lateral displacement in the x-direction (u_x) was more significant than the lateral displacement in the y-direction (u_y). The relationship between the axial load and lateral displacement response of columns with different channel slenderness ratios between batten plates (λ_z) is depicted in Figure 14. Once the short columns reach their peak strength, regarded as insignificant, their axial strength significantly decreases. The column with a higher slenderness ratio exhibited more, excellent ductility than those with a smaller slenderness ratio. Therefore, the ductility of the column was directly correlated with the overall slenderness ratio. The lateral displacement (Δ) at which the columns reached their maximum axial strengths are normalized relative to their length (L). The axial stiffness of a column is evident when it is subjected to axial load, with column dimensions of $D/B = 0.70$ and 0.75 .

Meanwhile, columns subjected to the axial stiffness were inversely proportional to the overall slenderness ratio for an axial load with the same column depth-to-width ratio (D/B).

Additionally, the axial stiffness of the columns with channel slenderness ratios between batten plates (λ_z) of 11.29 was higher than that of the columns with slenderness ratios of 21.94 and 29.03.

Due to the absence of stiffeners in the chord members of the built-up columns, which are made of unstiffened CFS channel sections, these columns are prone to local buckling failures. As a result, the normalized lateral displacements of the columns showed a scattered upward trend. Similarly, increasing the channel slenderness ratios between batten plates (λ_z) leads to higher lateral drift before failure and significantly reduces scattering.



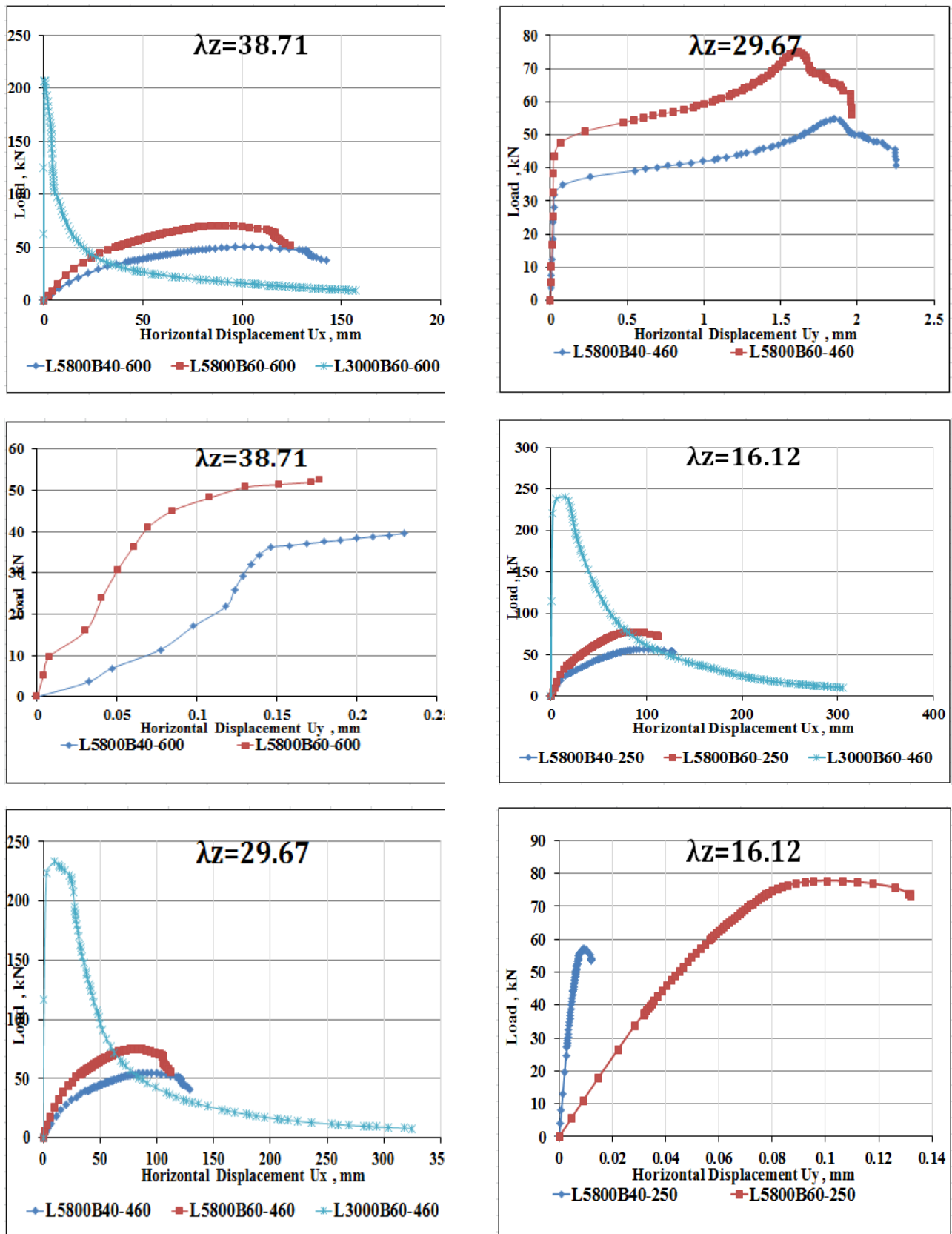


Figure 14: The relationships between load and lateral displacement (Ux) and (Uy) for columns subjected to a xial loads.

VI. CONCLUSION

The investigation utilized a nonlinear finite element model to analyze the ultimate capacity of battened columns composed of two thin channel sections arranged in a back-to-back configuration. The models accounted for both geometric and material nonlinearities.

For axially loaded columns, the failure modes varied based on column length:

Short columns: Local buckling was the primary failure mode.

Long columns: Flexural buckling dominated failure.

Intermediate columns: Failure occurred due to interactive buckling (a combination of local and flexural buckling).

Finite element results for short and slender battened columns closely matched EC3 and AISI-LRFD specifications. Medium columns predominantly failed due to local and flexural buckling. For sections with a high slenderness ratio, EC3 and AISI-LRFD predictions were not conservative, with EC3 being less reliable than AISI.

Geometrical imperfections ($\Delta = L/1000$) were incorporated in all loading cases, including axially loaded members.

Failure behavior varied based on buckling type:

Local buckling: The Direct Strength Method (DSM) provided un-conservative results, while Global buckling: DSM results were slightly conservative.

According to EC3, open sections yielded conservative predictions for local buckling and slightly conservative predictions for global buckling. However, Uniaxially loaded columns demonstrated the opposite behavior.

For column cross-sections with intermediate slenderness ratios (λ_c), the strength reduction exhibited a concave downward relationship, with maximum strength reduction occurring under primarily axial compressive loading.

Furthermore, the ultimate strength was negatively impacted by both the slenderness ratio of channels between batten plates (λ_z) and large back-to-back distances between channel sections.

Conflicts of Interest: The authors declare no conflict of interest.

REFERENCES

- [1] D. C. Fratafico and B. W. Schafer, "Numerical studies on the composite action and buckling behavior of built-up cold-formed steel columns," in 22nd International Specialty Conference on Cold-Formed Steel Structures, 2014.
- [2] ABAQUS Analysis User's Manual-Version 6.16, USA: ABAQUS Inc., 2016.
- [3] C. Yu and B. W. Schafer, "Simulation of cold-formed steel beams in local and distortional buckling with applications to the direct strength method," *Journal of Constructional Steel Research*, vol. 63, pp. 581-590, 2007.
- [4] Y. Li, Y. Li, S. Wang, and Z. Shen, "Ultimate load-carrying capacity of cold-formed thin-walled columns with built-up box and I section under axial compression," *Thin-Walled Structures*, vol. 79, pp.202-217, 2014.
- [5] M.T. Chen, B. Young, A.D. Martins, D. Camotim, P.B. Dinis, "Experimental investigation on cold-formed steel stiffened lipped channel columns undergoing local-distortional interaction," *Thin-Walled Struct.* 150 (2020) 106682.
- [6] Roy, K., Ting, T.C.H., Lau, H.H., Lim, J.B.P. (2018) "Nonlinear behavior of back-to-back gapped built-up cold-formed steel channel sections under compression," *Journal on Constructional Steel Research*, 147 257-276.
- [7] Krishanu Roy, Hieng Ho Lau, et al. "Experiments and finite element modelling of screw pattern of self-drilling screw connections for high strength cold-formed steel," *Thin-Walled Structures* 145 (2019) 106393.
- [8] M.A. El-Aghoury, A.H. Salem, M.T. Hanna, E.A. Amoush, "Experimental investigation for the behavior of battened beam-columns composed of four equal slender angles," *Thin-Walled Struct.* 48 (9) (2010) 669–683.
- [9] M. Anbarasu, "Behavior of cold-formed steel built-up battened columns composed of four lipped angles: tests and numerical validation," *Adv. Struct. Eng.* 23 (1) (2020) 51–64.
- [10] AISI S-100, "North American Specification for the Design of Cold-Formed Steel Structural Members," AISI Standard, Washington, DC, 2016.
- [11] EN 1993-1-3, Eurocode 3: "Design of Steel Structures. Design of Steel Structures. Part 1–3: General Rules – Supplementary Rules for Cold-Formed Members and Sheeting," European Committee for Standardization, Brussels, 2006.
- [12] S. Kherbouche, A. Megnounif, "Numerical study and design of thin-walled cold-formed steel built-up open and closed section columns," *Eng. Struct.* 179 (15) (2019) 670–682.
- [13] M.A. Dar, D.R. Sahoo, A.K. Jain, "Influence of chord compactness and slenderness on axial compression behavior of built-up battened CFS columns," *J. Build. Eng.* 32 (2020), 101743.
- [14] S. Vijayanand, M. Anbarasu, "Parametric study and improved design guidelines of CFS battened built-up columns," *Steel Compos. Struct.* 40 (5) (2021) 733–746.
- [15] S. Vijayanand, M. Anbarasu, "Behavior of CFS built-up battened columns: parametric study and design recommendations," *Struct. Eng. Mech.* 74 (3) (2020) 381–394.
- [16] X. Zhou, Y. Xiang, Y. Shi, L. Xu, Y. Zou, "Simplified design method of cold-formed steel columns with built-up box sections," *Eng. Struct.* 228 (2021), 111532.
- [17] S. Nie, T. Zhou, M.R. Eatherton, J. Li, Y. Zhang, "Compressive behavior of built-up double-box columns consisting of four cold-formed steel channels," *Eng. Struct.* 222 (2020), 111133.
- [18] S. Kechidi, D.C. Fratafico, B.W. Schafer, J.M. Castro, Bourahla., "Simulation of screw connected built-up cold-formed steel back-to-back lipped channels under axial compression," *Eng. Struct.* 206 (2020) 110109.
- [19] H. Luo, J. Liu, C. Li, K. Chen, M. Zhang, "Ultra-rapid delivery of specialty field hospitals to combat COVID-19: lessons learned from the Leishenshan hospital project in Wuhan," *Autom. Constr.* 119 (2020), 103345.
- [20] M. Dabaon, E. Ellobody, K. Ramzy, "Experimental investigation of built-up cold formed steel section battened columns," *Thin-Walled Struct.* 92 (2015) 137–145.



[21] ASCE. Minimum design loads for buildings and other structures,” ASCE/SEI 7-05.American Society of Civil Engineers Standard; 2006.

[22] M. Adil Dar a, Abhishek Verma b, et al, “Design of cold-formed steel battened built-up columns,” Journal of Constructional Steel Research 193 (2022) 107291